# Purely functional distributed 

 programmingfor collaborative applications.
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## Why is writing this application hard?



Not enough functional programming!

Please ask questions!

## ping

```
client(Pid) ->
    {server, Pid} ! {ping,self()};
    receive
        pong ->
        client(Pid)
    end.
```

```
server()
    receive
        {ping, Pid} ->
        Pid ! pong;
        server()
    end.
```


## ping

client(Pid) ->
\{server, Pid\} ! \{ping,self()\};
receive
end. better than


What is a distributed program?
"places"
"moments"

(8) A)

Space
Time

## Spacetime $\rightarrow a$

## temperature :: Spacetime $\rightarrow$ Kelvin

Relativistic Functional Reactive Programming

Behavior $a=$ Spacetime $\rightarrow a$
Event $a=$ Map Spacetime $a$

# Relativistic Functional Reactive Programming <br> Conal Elliott \& Paul Hudak, 1997 

## Behavior $a=$ Spacetime $\rightarrow a$

Event $a=$ Map Spacetime $a$

What about communication?





Facts travel together to avoid modeling partial transmission of information.


## all-knowi transitive



## C <br> D

## ping through the lens of perception

```
Client Server
```



```
ping : Event ()
```

ping : Event ()
ping =
ping =
perceptionsAt client
perceptionsAt client
(perceptionsAt server
(perceptionsAt server
(canYouHearMe <> ping)
(canYouHearMe <> ping)
canYouHearMe : Event ()
canYouHearMe : Event ()
canYouHearMe = { c1 }
canYouHearMe = { c1 }
ping : Event ()
ping : Event ()
ping = { c2, c3, c4, ... }

```
ping = { c2, c3, c4, ... }
```


## Location-free programming

Client

## Somewhere <br> Else

```
pingish : Event () -> Event ()
pingish start =
    perceptions
            (perceptions
                            (start <> pingish)
ping : Event () -> Event ()
ping start =
at client
    (restrict [client, server]
    (pingish start))
```


## Location-free programming

Client
Server
Somewhere
Else

```
pingish : Event () -> Event ()
pingish start =
    perceptions
    (perceptions
        (start <> pingish)
ping : Event () -> Event ()
ping start =
    at client
    (restrict [client, server]
    (pingish start))
```


# Relativistic Functional Reactive Programming 

Behavior a = Spacetime $\rightarrow a$
Event a = Map Spacetime a

It rains, thus the ground is wet.


Facts travel together to avoid modeling partial transmission of information.

Perception is transitive

$$
a<b \wedge b<c \Rightarrow a<c
$$



$$
\text { 回 } 0
$$




## Strong Eventual Consistency

"predictably derive a result from known operations"
"predictably derive a result from known operations"

"predictably derive a result from known operations"





## Is "Fix solar panels" deleted?

$\begin{aligned} & \text { fold (||) False }\left\{\begin{array}{ccc}\text { True } & \text { True } & \text { False } \\ & & \text { True || True || False } \\ & =\text { True }\end{array}\right. \\ &\end{aligned}$

Conflict-Free Replicated Data Types
type Crdt operations values =
Event operations $\rightarrow$ Behavior values

## Enable-Once Flag CRDT

eoflag :: Crdt Bool Bool eoflag = fold (||) False



## Do the solar panels need fixing?


"Overriding" decisions?


## $\Rightarrow$ True

Last-Wr -Wins

## True

$$
\begin{gathered}
\{0, \bullet\} \\
0<\bullet
\end{gathered}
$$

False ©


- False

Concurrent events
concurrent : : Event a $\rightarrow$ Behavior (Event a)


## Do the solar panels need fixing?


$(=\ll):$ Behavior $\mathrm{a} \rightarrow(\mathrm{a} \rightarrow$ Behavior b$) \rightarrow$ Behavior b

Enable-Once Flag CRDT eoflag :: Crdt Bool Bool eoflag = fold (||) False

Enable-Wins Flag CRDT
ewflag :: Crdt Bool Bool ewflag = (eoflag =<< concurrent)

## $x$ Fix solar panels

## Fix solar panels

$\begin{array}{lll}\text { 1. Insert 'x' @ } 10 & \neq & \text { 1. Insert 'y' @ } 10 \\ \text { 2. Insert 'y' @ } 10 & \text { 2. Insert 'x' @ } 10\end{array}$

## Fix solar xypanels

## Fix solar yxpanels


insert ' $x$ ' between $(1,2) \quad$ insert ' $y$ ' between $(2,3)$

## $a^{1} x^{4} b^{2} y^{5} c^{3}$



## topologicalSort <br> $[\underset{\mathrm{a}}{ } \mathrm{b}$

[ab] or [ba]?

Tie breaking on identifiers

Let's program sequences!
sequence :: Event (Pos, Pos, a)
$\rightarrow$ Behavior [(Id, a)]
$\uparrow$
data Pos = Start
| Middle Id End
type Id = Spacetime
tagWithSpacetime :: Event a
$\rightarrow$ Event (Spacetime, a)
sequence : : Event (Pos, Pos, $a$ )
$\rightarrow$ Behavior [(Id, a)]
sequence e =
let idsE = tagWithSpacetime e
graphB $=$ fold Set. union Set.empty (mapE Set.singleton idsE)
in mapB topologicalSort graphB
topologicalSort :: Set (Id, (Pos, Pos, a))
$\rightarrow[(\mathrm{Id}, a)]$
mapE $::(a \rightarrow b) \rightarrow$ Event $a \rightarrow$ Event $b$
mapB $::(a \rightarrow b) \rightarrow$ Behavior $a \rightarrow$ Behavior $b$

Sequence with deletion

$$
\begin{aligned}
\text { sequence } & :: \text { Event (Pos, Pos, a) } \\
& \rightarrow \text { Behavior }[(\operatorname{Id}, a)]
\end{aligned}
$$

$$
a=\text { Behavior (Bool, } a^{\prime} \text { ) }
$$

$\longrightarrow$ Behavior [(Id, Behavior Bool $a)$ ] $\quad \begin{aligned} & \text { filter }+(=\ll) \leadsto \text { Behavior }[(I d, a)]\end{aligned}$

$\times$ Fix solar panels

enable-wins
flag
sequence + enable-once flag

WIP
Eventually Consistent
RFRP

- Library UX for GUI
- Extending Reflex!
https://github.com/reflex-frp/reflex
=> Production quality P2P apps
- Hard problems (PhD)

Sequence with deletion

$$
\begin{aligned}
\text { sequence } & :: \text { Event (Pos, Pos, a) } \\
& \rightarrow \text { Behavior }[(\operatorname{Id}, a)]
\end{aligned}
$$

$$
a=\text { Behavior (Bool, } a^{\prime} \text { ) }
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$\longrightarrow$ Behavior [(Id, Behavior Bool $a)$ ] $\quad \begin{aligned} & \text { filter }+(=\ll) \leadsto \text { Behavior }[(I d, a)]\end{aligned}$

## Relativistic Functional Reactive Programming

Behavior a = Spacetime $\rightarrow a$ Event a = Map Spacetime a

$$
\begin{aligned}
\text { fold } & ::(a \rightarrow a \rightarrow a) \quad \text { (Commutative \& associative) } \\
& \rightarrow \text { a } \\
& \rightarrow \text { Event a } \\
& \rightarrow \text { Behavior a }
\end{aligned}
$$

concurrent : : Event a
$\rightarrow$ Behavior (Event a)

Peer-to-peer apps for free!

Probabilistic
Relativistic
Functional Reactive Programming

## Behavior $a \rightarrow$ (Spacetime, Probability, $a$ )

temperature :: Spacetime $\rightarrow$ Kelvin


